

**LESSON**  
**16-1**

**Properties of Logarithms**

*Practice and Problem Solving: A/B*

**Express as a single logarithm. Simplify, if possible.**

1.  $\log_3 9 + \log_3 27$

\_\_\_\_\_

2.  $\log_2 8 + \log_2 16$

\_\_\_\_\_

3.  $\log_{10} 80 + \log_{10} 125$

\_\_\_\_\_

4.  $\log_6 8 + \log_6 27$

\_\_\_\_\_

5.  $\log_3 6 + \log_3 13.5$

\_\_\_\_\_

6.  $\log_4 32 + \log_4 128$

\_\_\_\_\_

**Express as a single logarithm. Simplify, if possible.**

7.  $\log_2 80 - \log_2 10$

\_\_\_\_\_

8.  $\log_{10} 4000 - \log_{10} 40$

\_\_\_\_\_

9.  $\log_4 384 - \log_4 6$

\_\_\_\_\_

10.  $\log_2 1920 - \log_2 30$

\_\_\_\_\_

11.  $\log_3 486 - \log_3 2$

\_\_\_\_\_

12.  $\log_6 180 - \log_6 5$

\_\_\_\_\_

**Simplify, if possible.**

13.  $\log_4 4^6$

\_\_\_\_\_

14.  $\log_5 5^{x-5}$

\_\_\_\_\_

15.  $7^{\log_7 30}$

\_\_\_\_\_

16.  $12^{\log_{12} 1}$

\_\_\_\_\_

17.  $\log_8 8^5$

\_\_\_\_\_

18.  $\log_3 9^4$

\_\_\_\_\_

**Evaluate. Round to the nearest hundredth.**

19.  $\log_{12} 1$

\_\_\_\_\_

20.  $\log_3 30$

\_\_\_\_\_

21.  $\log_5 10$

\_\_\_\_\_

**Solve.**

22. The Richter magnitude of an earthquake,  $M$ , is related to the energy released in ergs,  $E$ , by the formula  $M = \frac{2}{3} \log \left( \frac{E}{10^{11.8}} \right)$ .

Find the energy released by an earthquake of magnitude 4.2. \_\_\_\_\_

**LESSON**  
**16-1**

**Properties of Logarithms**

*Practice and Problem Solving: C*

**Express as a single logarithm. Simplify, if possible.**

1.  $\log_6 12 + \log_6 18$

\_\_\_\_\_

2.  $\log_3 81 - \log_3 27$

\_\_\_\_\_

3.  $\log_4 128 - \log_4 8$

\_\_\_\_\_

4.  $\log_6 18 + \log_6 72$

\_\_\_\_\_

5.  $\log_5 3125 - \log_5 25$

\_\_\_\_\_

6.  $\log_8 128 + \log_8 256$

\_\_\_\_\_

7.  $\log_5 5 + \log_5 125$

\_\_\_\_\_

8.  $\log_2 256 - \log_2 64$

\_\_\_\_\_

9.  $\log_3 8019 - \log_3 99$

\_\_\_\_\_

10.  $\log_8 80 + \log_8 51.2$

\_\_\_\_\_

11.  $\log_7 13.3 - \log_7 1.9$

\_\_\_\_\_

12.  $\log_{10} 125 + \log_{10} 80$

\_\_\_\_\_

**Evaluate. Round to the nearest hundredth.**

13.  $\log_8 8^6$

\_\_\_\_\_

14.  $2^{\log_2 8^x}$

\_\_\_\_\_

15.  $\log_2 16^5$

\_\_\_\_\_

16.  $\log_3 3^{(2x+1)}$

\_\_\_\_\_

17.  $\log_4 16^{(x-1)}$

\_\_\_\_\_

18.  $5^{\log_5 17}$

\_\_\_\_\_

19.  $\log_3 5^2$

\_\_\_\_\_

20.  $\log_5 \left( \frac{1}{125} \right)^2$

\_\_\_\_\_

21.  $\log_6 \left( \frac{1}{6^4} \right)^3$

\_\_\_\_\_

22.  $\log_4 20^2$

\_\_\_\_\_

23.  $\log_9 27^4$

\_\_\_\_\_

24.  $\log_2 10$

\_\_\_\_\_

**Solve.**

25. Carmen has a painting presently valued at \$5000. An art dealer told her the painting would appreciate at a rate of 6% per year. In how many years will the painting be worth \$8000?

a. Write a logarithmic expression representing the situation. \_\_\_\_\_

b. Simplify your expression. How many years will it take? \_\_\_\_\_

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**MODULE 16 Logarithmic Properties and Exponential Equations****LESSON 16-1****Practice and Problem Solving: A/B**

1.  $\log_3 243 = 5$
2.  $\log_2 128 = 7$
3.  $\log_{10} 10,000 = 4$
4.  $\log_6 216 = 3$
5.  $\log_3 81 = 4$
6.  $\log_4 4096 = 6$
7.  $\log_2 8 = 3$
8.  $\log_{10} 100 = 2$
9.  $\log_4 64 = 3$
10.  $\log_2 64 = 6$
11.  $\log_3 243 = 5$
12.  $\log_6 36 = 2$
13. 6
14.  $x - 5$
15. 30
16. 1
17. 5
18. 8
19. 0
20. 3.10
21. 1.43
22.  $1.26(10)^{18}$  ergs

**Practice and Problem Solving: C**

1.  $\log_6 216 = 3$
2.  $\log_3 3 = 1$
3.  $\log_4 16 = 2$
4.  $\log_6 1296 = 4$
5.  $\log_5 125 = 3$
6.  $\log_8 32,768 = 5$
7.  $\log_5 625 = 4$
8.  $\log_2 4 = 2$
9.  $\log_3 81 = 4$
10.  $\log_8 4096 = 4$
11.  $\log_7 7 = 1$
12.  $\log_{10} 10,000 = 4$
13. 6
14.  $8^x$
15. 20

16.  $2x + 1$
17.  $2x - 2$
18. 17
19. 2.93
20. -6
21. -12
22. 4.32
23. 6
24. 3.32
25. a.  $\log_{1.06} 1.6$   
b. about 8 years

### Practice and Problem Solving: Modified

1. 4
2. 64; 64; 6
3. 3125; 3125; 5
4.  $\log_{10} 10,000 = 4$
5.  $\log_6 6 = 1$
6.  $\log_8 64 = 2$
7.  $\log_5 25 = 2$
8.  $\log_3 3 = 1$
9.  $\log_2 32 = 5$
10.  $\log_4 16 = 2$
11.  $\log_6 36 = 2$
12.  $\log_5 125 = 3$
13. 4
14. 4
15. 9
16. 4
17. 12
18. 2
19. 1.59
20. 1.77
21. 1.46
22.  $10^{22}$  ergs

### Reading Strategies

1. True; Product Property
2. True; Quotient Property
3. False; Power Property
4. False; Change of Base Property
5.  $5 \log x$ ; Power Property
6.  $\log x$ ; Quotient Property
7. 1; Product Property

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8.  $x \log x$ ; Power Property